

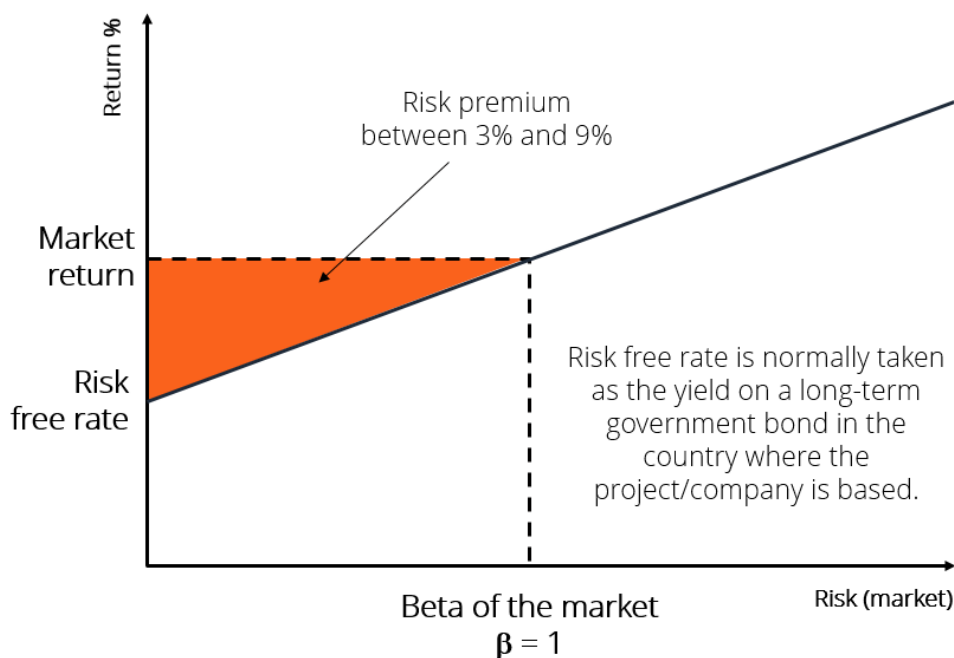
CAPM MODELING: RISK ESTIMATION AND MITIGATION ANALYSIS

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The capital asset pricing model (CAPM) is a model that portrays the connection between expected return and danger of a security. It demonstrates that the arrival on a security is equivalent to the hazard free return in addition to a hazard premium, which depends on the BETA of that security. The following is a delineation of the CAPM idea.

Capital Asset Pricing Model



All stocks can be analyzed and their relative study can be done using β (Risk Factor), α (Intercept), σ (Standard Deviation), σ^2 (Variance), R (Security Return), P/E Ratio (Price earnings Ratio), r (Correlation Coefficient), and r^2 (Variation).

P/E Ratio was the primary ratio on which basis analysis of the company is done, Standard Deviation for the short listed companies was compared, after that analysis returns of the respective company was compared and lastly short listing of company was completed after comparing their respective Risks.

1.1 Characteristic Regression Line (CRL) Analysis

Formula Used

$$\beta = \frac{n\sum XY - (\sum x)(\sum y)}{n\sum X^2 - (\sum X)^2}$$

$$\sigma = \sqrt{(\sum P[ri - E(r)]^2)}$$

$$\alpha = \bar{Y} - \beta \bar{X}$$

$$\text{Variance} = \sigma^2$$

$$R = \frac{Pt - Pt-1}{Pt-1}$$

$$r = \frac{n\sum XY - (\sum X)(\sum Y)}{\sqrt{(n\sum X^2 - (\sum X)^2)}\sqrt{(n\sum Y^2 - (\sum Y)^2)}}$$

$$\text{P/E Ratio} = \frac{Pi}{EPS}$$

$$\text{Variation} = r^2$$

Where

β = Risk Factor

α = Intercept

σ = Standard Deviation

σ^2 = Variance

R = Security Return

P/E Ratio = Price earnings Ratio

r = Correlation Coefficient

r^2 = Variation

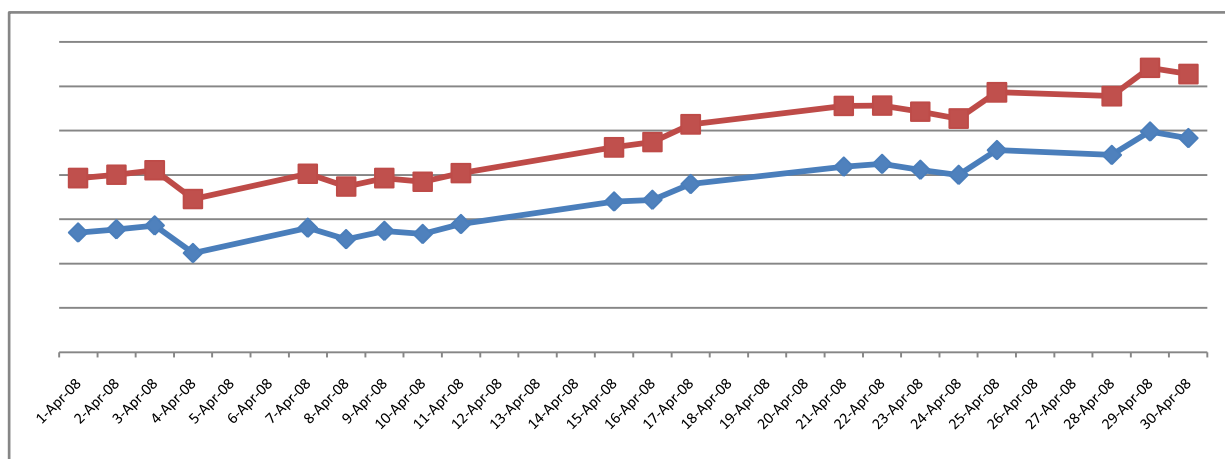
1.2 Beta (β), Security Return (R_i), and Correlation (r) Calculation**1.2.1. HCL****Beta (β), Security Return (R_i), and Correlation (r) Calculation**

S No.	Date	NIFTY	HCL	Index reten(X)	X ²	Stock return(Y)	Y ²	X*Y
		4739.5						
	1-Apr-08	5	246.3					
1	2-Apr-08	4754.2	247	0.3091	0.0955	0.2842	0.0808	0.0878
			249.8					
2	3-Apr-08	4771.6	5	0.3660	0.1340	1.1538	1.3314	0.4223
3	4-Apr-08	4647	244.9	-2.6113	6.8188	-1.9812	3.9251	5.1734
			244.5					
4	7-Apr-08	4761.2	5	2.4575	6.0393	-0.1429	0.0204	-0.3512
		4709.6	238.6					
5	8-Apr-08	5	5	-1.0827	1.1723	-2.4126	5.8206	2.6121
		4747.0						
6	9-Apr-08	5	239	0.7941	0.6306	0.1467	0.0215	0.1165
7	10-Apr-08	4733	236.6	-0.2960	0.0876	-1.0042	1.0084	0.2972
8	11-Apr-08	4777.8	230.4	0.9465	0.8959	-2.6205	6.8668	-2.4804
		4879.6						13.508
9	15-Apr-08	5	245	2.1317	4.5443	6.3368	40.1551	4
10	16-Apr-08	4887.3	260.5	0.1568	0.0246	6.3265	40.0250	0.9918
11	17-Apr-08	4958.4	269.6	1.4548	2.1164	3.4933	12.2030	5.0820
12	21-Apr-08	5037	274.3	1.5852	2.5128	1.7433	3.0392	2.7635
			263.6					
13	22-Apr-08	5049.3	5	0.2442	0.0596	-3.8826	15.0747	-0.9481
			262.4					
14	23-Apr-08	5022.8	5	-0.5248	0.2754	-0.4551	0.2072	0.2389
		4999.8						
15	24-Apr-08	5	254.1	-0.4569	0.2088	-3.1816	10.1223	1.4537
16	25-Apr-08	5111.7	260.7	2.2371	5.0045	2.5974	6.7465	5.8106
		5089.6						
17	28-Apr-08	5	265.4	-0.4314	0.1861	1.8028	3.2502	-0.7777
								16.847
18	29-Apr-08	5195.5	286.9	2.0797	4.3252	8.1010	65.6259	7
			288.4					
19	30-Apr-08	5165.9	5	-0.5697	0.3246	0.5403	0.2919	-0.3078
sum=				8.7899	35.4563	16.8455	215.815	50.540
							9	8

Beta(β)=	1.3618	Stock Return=	9.00%
Alfa(α)=	0.2566	\bar{X} =	0.4626
Standard Error(e)=	0.0266	\bar{y} =	0.8866
	6	Beta* \bar{X}	=
			0.6300

Stock Return(R)=	0.41
Expected Return=	0.84

Correlation(r)		Percentage Variation(r^2)	
=	0.56	=	31.57



Calculation For Standard Deviation And Expected Stock Return

Standard Deviation For Stock				Expected Return
1.30	1.69	0.05	0.08	
2.00	4.00	0.05	0.20	0.01
4.85	23.52	0.05	1.18	0.06
-0.10	0.01	0.05	0.00	-0.10
-0.45	0.20	0.05	0.01	-0.01
-6.35	40.32	0.05	2.02	-0.12
-6.00	36.00	0.05	1.80	0.01
-8.40	70.56	0.05	3.53	-0.05

Standard Deviation for Index			
-140.1	19628.01	0.05	981.40
-			
125.45	15737.70	0.05	786.89
-			
108.05	11674.80	0.05	583.74
-			
232.65	54126.02	0.05	2706.30
-			
118.45	14030.40	0.05	701.52
-			
-170	28900.00	0.05	1445.00
-			
-132.6	17582.76	0.05	879.14
-			
146.65	21506.22	0.05	1075.31

-				
14.60	213.16	0.05	10.66	-0.13
0.00	0.00	0.05	0.00	0.32
15.50	240.25	0.05	12.01	0.32
24.60	605.16	0.05	30.26	0.17
29.30	858.49	0.05	42.92	0.09
18.65	347.82	0.05	17.39	-0.19
17.45	304.50	0.05	15.23	-0.02
9.10	82.81	0.05	4.14	-0.16
15.70	246.49	0.05	12.32	0.13
20.40	416.16	0.05	20.81	0.09
41.90	1755.61	0.05	87.78	0.41
43.45	1887.90	0.05	94.40	0.03
			356.73	0.84
	Variance=	356.73		
	SD=	18.89%		

-			
101.85	10373.42	0.05	518.67
0	0.00	0.05	0.00
7.65	58.52	0.05	2.93
78.75	6201.56	0.05	310.08
157.35	24759.02	0.05	1237.95
169.65	28781.12	0.05	1439.06
143.15	20491.92	0.05	1024.60
120.2	14448.04	0.05	722.40
232.05	53847.20	0.05	2692.36
210	44100.00	0.05	2205.00
315.85	99761.22	0.05	4988.06
286.25	81939.06	0.05	4096.95
			28397.35
	Variance=	28397.35	
	SD=	168.52%	

1.2.2. INFOSYS

Beta (β), Security Return (Ri), and Correlation (r) Calculation

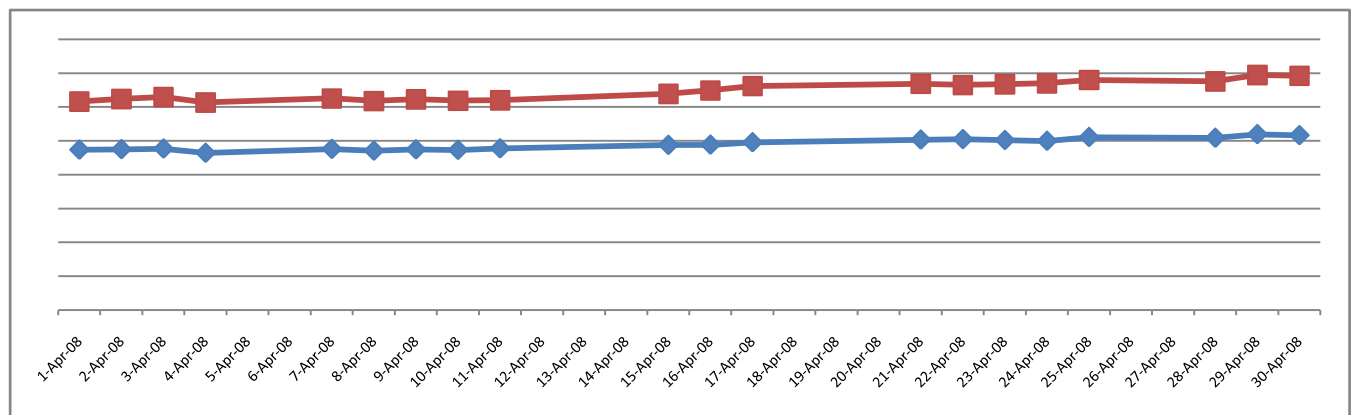
S No.	Date	NIFTY	Infosys	Index reten(X)	X*X	Stock return(Y)	Y*Y	X*Y
	1-Apr-08	4739.55	1423.05					
1	2-Apr-08	4754.2	1482.8	0.3091	0.0955	4.1987	17.6293	1.2978
2	3-Apr-08	4771.6	1522.5	0.3660	0.1340	2.6774	7.1683	0.9799
3	4-Apr-08	4647	1485.45	-2.6113	6.8188	-2.4335	5.9219	6.3546
4	7-Apr-08	4761.2	1492.05	2.4575	6.0393	0.4443	0.1974	1.0919
5	8-Apr-08	4709.65	1466.95	-1.0827	1.1723	-1.6822	2.8300	1.8214
6	9-Apr-08	4747.05	1479.95	0.7941	0.6306	0.8862	0.7853	0.7037
7	10-Apr-08	4733	1452.6	-0.2960	0.0876	-1.8480	3.4152	0.5470
8	11-Apr-08	4777.8	1421.9	0.9465	0.8959	-2.1135	4.4667	-2.0005
9	15-Apr-08	4879.65	1510.4	2.1317	4.5443	6.2241	38.7390	13.2681
10	16-Apr-08	4887.3	1600.2	0.1568	0.0246	5.9454	35.3483	0.9321
11	17-Apr-08	4958.4	1659.1	1.4548	2.1164	3.6808	13.5482	5.3548
12	21-Apr-08	5037	1645.8	1.5852	2.5128	-0.8016	0.6426	-1.2707
13	22-Apr-08	5049.3	1598.6	0.2442	0.0596	-2.8679	8.2249	-0.7003
14	23-Apr-08	5022.8	1647.95	-0.5248	0.2754	3.0871	9.5300	-1.6202
15	24-Apr-08	4999.85	1696.05	-0.4569	0.2088	2.9188	8.5193	-1.3336
16	25-Apr-08	5111.7	1684.3	2.2371	5.0045	-0.6928	0.4800	-1.5498

17	28-Apr-08	5089.65	1663.65	-0.4314	0.1861	-1.2260	1.5031	0.5289
18	29-Apr-08	5195.5	1749.55	2.0797	4.3252	5.1633	26.6601	10.7383
19	30-Apr-08	5165.9	1753.1	-0.5697	0.3246	0.2029	0.0412	-0.1156
sum=				8.7899	35.4563	21.7634	185.6509	35.0275

Beta =	0.7951	Stock Return=	9.00%
Alfa =	0.7776	\bar{X} =	0.4626
Standard Error(e)=	0.02666	\bar{y} =	1.1454
		Beta* \bar{X} =	0.3679

Stock Return(R)=	0.88
Expected Return=	1.09

Correlation(r)=	0.369909511	Percentage Variation(r*r)=	0.136833046
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Calculation For Standard Deviation And Expected Stock Return

Standard Deviation For Stock				Expected Return
-87.35	7630.02	0.05	381.50	
-27.60	761.76	0.05	38.09	0.21
12.10	146.41	0.05	7.32	0.13
-24.95	622.50	0.05	31.13	-0.12
-18.35	336.72	0.05	16.84	0.02
-43.45	1887.90	0.05	94.40	-0.08
-30.45	927.20	0.05	46.36	0.04

Standard Deviation for Index			
-140.1	19628.01	0.05	981.40
-			
125.45	15737.70	0.05	786.89
-			
108.05	11674.80	0.05	583.74
-			
232.65	54126.02	0.05	2706.30
-			
118.45	14030.40	0.05	701.52
-170	28900.00	0.05	1445.00
-132.6	17582.76	0.05	879.14

-57.80	3340.84	0.05	167.04	-0.09
-88.50	7832.25	0.05	391.61	-0.11
0.00	0.00	0.05	0.00	0.31
89.80	8064.04	0.05	403.20	0.30
148.70	22111.69	0.05	1105.58	0.18
135.40	18333.16	0.05	916.66	-0.04
88.20	7779.24	0.05	388.96	-0.14
137.55	18920.00	0.05	946.00	0.15
185.65	34465.92	0.05	1723.30	0.15
173.90	30241.21	0.05	1512.06	-0.03
153.25	23485.56	0.05	1174.28	-0.06
239.15	57192.72	0.05	2859.64	0.26
242.70	58903.29	0.05	2945.16	0.01
			15149.12	1.09
Variance=		15149.12		
SD=		123.08%		

-	146.65	21506.22	0.05	1075.31
-	101.85	10373.42	0.05	518.67
0	0.00	0.00	0.05	0.00
7.65	58.52	0.05	0.05	2.93
78.75	6201.56	0.05	0.05	310.08
157.35	24759.02	0.05	0.05	1237.95
169.65	28781.12	0.05	0.05	1439.06
143.15	20491.92	0.05	0.05	1024.60
120.2	14448.04	0.05	0.05	722.40
232.05	53847.20	0.05	0.05	2692.36
210	44100.00	0.05	0.05	2205.00
315.85	99761.22	0.05	0.05	4988.06
286.25	81939.06	0.05	0.05	4096.95
				28397.35
Variance=		28397.35		
SD=		168.52%		

1.2.4. TCS

Beta (β), Security Return (Ri), and Correlation (r) Calculation

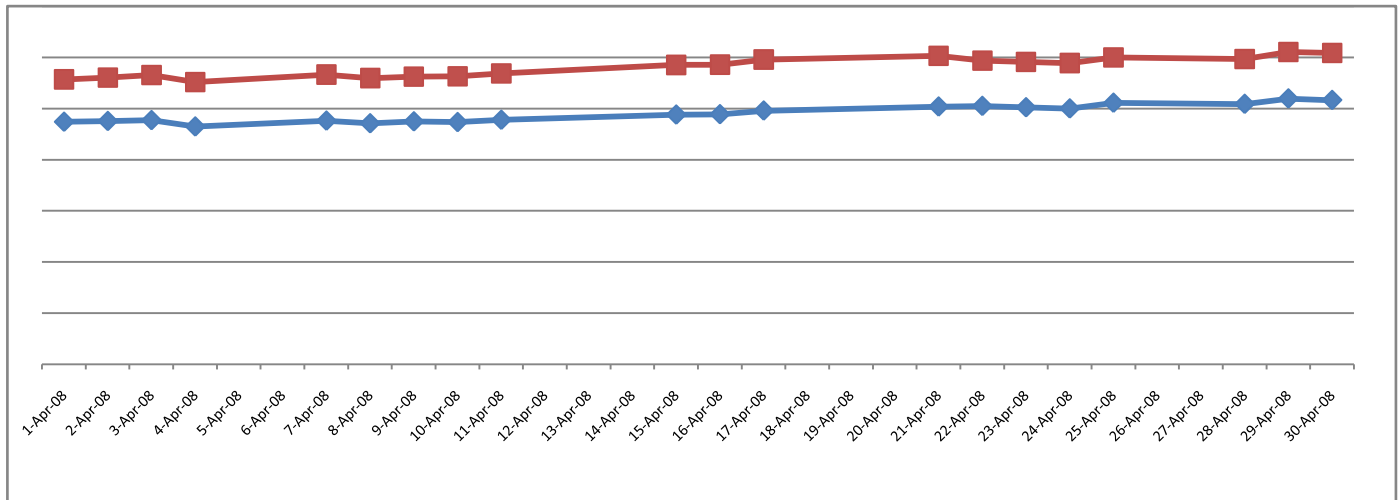
S No.	Date	NIFTY	TCS	Index reten(X)	X*X	Stock return(Y)	Y*Y	X*Y
	1-Apr-08	4739.55	832.35					
1	2-Apr-08	4754.2	851.25	0.3091	0.0955	2.2707	5.1560	0.7019
2	3-Apr-08	4771.6	885.4	0.3660	0.1340	4.0117	16.0941	1.4683
3	4-Apr-08	4647	872.9	-2.6113	6.8188	-1.4118	1.9932	3.6866
4	7-Apr-08	4761.2	904.1	2.4575	6.0393	3.5743	12.7756	8.7838
5	8-Apr-08	4709.65	887.35	-1.0827	1.1723	-1.8527	3.4324	2.0059
6	9-Apr-08	4747.05	876.25	0.7941	0.6306	-1.2509	1.5648	-0.9934
7	10-Apr-08	4733	899.55	-0.2960	0.0876	2.6591	7.0706	-0.7870
8	11-Apr-08	4777.8	908	0.9465	0.8959	0.9394	0.8824	0.8891
9	15-Apr-08	4879.65	974.15	2.1317	4.5443	7.2852	53.0748	15.5302
10	16-Apr-08	4887.3	971.9	0.1568	0.0246	-0.2310	0.0533	-0.0362
11	17-Apr-08	4958.4	1000.9	1.4548	2.1164	2.9838	8.9033	4.3409
12	21-Apr-08	5037	993.4	1.5852	2.5128	-0.7493	0.5615	-1.1878
13	22-Apr-08	5049.3	887.2	0.2442	0.0596	-10.6906	114.2880	-2.6106
14	23-Apr-08	5022.8	889.15	-0.5248	0.2754	0.2198	0.0483	-0.1154
15	24-Apr-08	4999.85	890.75	-0.4569	0.2088	0.1799	0.0324	-0.0822
16	25-Apr-08	5111.7	889.3	2.2371	5.0045	-0.1628	0.0265	-0.3642
17	28-Apr-08	5089.65	881.7	-0.4314	0.1861	-0.8546	0.7303	0.3686
18	29-Apr-08	5195.5	910.55	2.0797	4.3252	3.2721	10.7066	6.8050

19	30-Apr-08	5165.9	921	-0.5697	0.3246	1.1477	1.3171	-0.6538
sum=				8.7899	35.4563	11.3401	238.7112	37.7498

Beta =	1.0355	Stock Return=	9.00%
Alfa =	0.1178	\bar{X} =	0.4626
Standard Error(e)=	0.02666	\bar{y} =	0.5968
		Beta* \bar{X} =	0.4790

Stock Return(R)=	0.24
Expected Return=	0.57

Correlation(r)=	0.393330066	Percentage Variation(r*r)=	0.154708541
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Calculation For Standard Deviation And Expected Stock Return

Standard Deviation For Stock				Expected Return
-141.80	20107.24	0.05	1005.36	
-122.90	15104.41	0.05	755.22	0.11
-88.75	7876.56	0.05	393.83	0.20
-101.25	10251.56	0.05	512.58	-0.07
-70.05	4907.00	0.05	245.35	0.18
-86.80	7534.24	0.05	376.71	-0.09
-97.90	9584.41	0.05	479.22	-0.06
-74.60	5565.16	0.05	278.26	0.13
-66.15	4375.82	0.05	218.79	0.05
0.00	0.00	0.05	0.00	0.36
-2.25	5.06	0.05	0.25	-0.01
26.75	715.56	0.05	35.78	0.15
19.25	370.56	0.05	18.53	-0.04
-86.95	7560.30	0.05	378.02	-0.53
-85.00	7225.00	0.05	361.25	0.01
-83.40	6955.56	0.05	347.78	0.01
-84.85	7199.52	0.05	359.98	-0.01
-92.45	8547.00	0.05	427.35	-0.04
-63.60	4044.96	0.05	202.25	0.16
-53.15	2824.92	0.05	141.25	0.06
			6537.74	0.57
	Variance=	6537.74		
	SD=	80.86%		

Standard Deviation for Index			
-140.1	19628.01	0.05	981.40
-125.45	15737.70	0.05	786.89
-108.05	11674.80	0.05	583.74
-232.65	54126.02	0.05	2706.30
-118.45	14030.40	0.05	701.52
-170	28900.00	0.05	1445.00
-132.6	17582.76	0.05	879.14
-146.65	21506.22	0.05	1075.31
-101.85	10373.42	0.05	518.67
0	0.00	0.05	0.00
7.65	58.52	0.05	2.93
78.75	6201.56	0.05	310.08
157.35	24759.02	0.05	1237.95
169.65	28781.12	0.05	1439.06
143.15	20491.92	0.05	1024.60
120.2	14448.04	0.05	722.40
232.05	53847.20	0.05	2692.36
210	44100.00	0.05	2205.00
315.85	99761.22	0.05	4988.06
286.25	81939.06	0.05	4096.95
			28397.35
	Variance=	28397.35	
	SD=	168.52%	

1.2.5. WIPRO

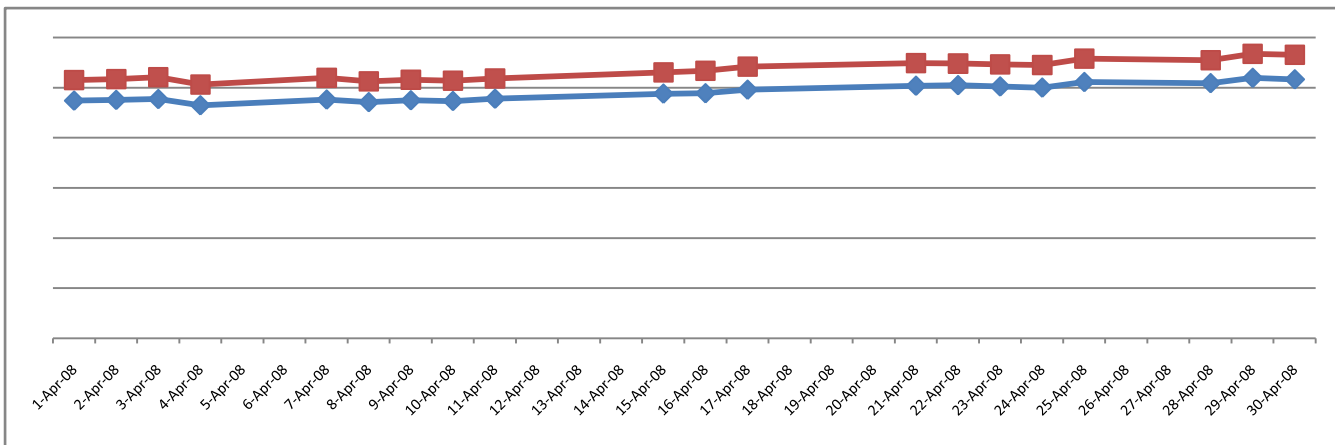
Beta (β), Security Return (R_i), and Correlation (r) Calculation

S No.	Date	NIFTY	Wipro	Index reten(X)	X*X	Stock return(Y)	Y*Y	X*Y
	1-Apr-08	4739.55	409.4					
1	2-Apr-08	4754.2	415.25	0.3091	0.0955	1.4289	2.0418	0.4417
2	3-Apr-08	4771.6	436.35	0.3660	0.1340	5.0813	25.8194	1.8597
3	4-Apr-08	4647	414.9	-2.6113	6.8188	-4.9158	24.1649	12.8365
4	7-Apr-08	4761.2	434.65	2.4575	6.0393	4.7602	22.6593	11.6981
5	8-Apr-08	4709.65	413.9	-1.0827	1.1723	-4.7740	22.7907	5.1688
6	9-Apr-08	4747.05	410.95	0.7941	0.6306	-0.7127	0.5080	-0.5660
7	10-Apr-08	4733	407.25	-0.2960	0.0876	-0.9004	0.8106	0.2665
8	11-Apr-08	4777.8	405.5	0.9465	0.8959	-0.4297	0.1847	-0.4067
9	15-Apr-08	4879.65	423.9	2.1317	4.5443	4.5376	20.5899	9.6730
10	16-Apr-08	4887.3	447.3	0.1568	0.0246	5.5202	30.4723	0.8654
11	17-Apr-08	4958.4	459.25	1.4548	2.1164	2.6716	7.1374	3.8866
12	21-Apr-08	5037	454.8	1.5852	2.5128	-0.9690	0.9389	-1.5360
13	22-Apr-08	5049.3	431.2	0.2442	0.0596	-5.1891	26.9267	-1.2671
14	23-Apr-08	5022.8	443.15	-0.5248	0.2754	2.7713	7.6803	-1.4545
15	24-Apr-08	4999.85	449.7	-0.4569	0.2088	1.4781	2.1846	-0.6753
16	25-Apr-08	5111.7	466.35	2.2371	5.0045	3.7025	13.7083	8.2827
17	28-Apr-08	5089.65	458.1	-0.4314	0.1861	-1.7691	3.1296	0.7631
18	29-Apr-08	5195.5	478.9	2.0797	4.3252	4.5405	20.6161	9.4429
19	30-Apr-08	5165.9	488.75	-0.5697	0.3246	2.0568	4.2304	-1.1718
sum=				8.7899	35.4563	18.8892	236.5937	58.1075

Beta =	1.5728		Stock Return=	9.00%	
Alfa =	0.2666	\bar{X} =	0.4626	\bar{y} =	0.9942
Standard Error(e)=	0.02666			Beta* \bar{X} =	0.7276

Stock Return(R)=	0.43
Expected Return=	0.94

Correlation(r)=	0.62099584	Percentage Variation(r^2)=	0.38563583
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Calculation For Standard Deviation And Expected Stock Return

Standard Deviation For Stock				Expected Return
-	14.50	210.25	0.05	
-	-8.65	74.82	0.05	3.74
-	12.45	155.00	0.05	7.75
-	-9.00	81.00	0.05	4.05
-	10.75	115.56	0.05	5.78
-	10.00	100.00	0.05	5.00
-	12.95	167.70	0.05	8.39
-	16.65	277.22	0.05	13.86
-	18.40	338.56	0.05	16.93
-	0.00	0.00	0.05	0.00
-	23.40	547.56	0.05	27.38
-	35.35	1249.62	0.05	62.48
-	30.90	954.81	0.05	47.74
-	7.30	53.29	0.05	2.66
-	19.25	370.56	0.05	18.53
-	25.80	665.64	0.05	33.28
-	42.45	1802.00	0.05	90.10

Standard Deviation for Index				
-	140.1	19628.01	0.05	981.40
-	125.45	15737.70	0.05	786.89
-	108.05	11674.80	0.05	583.74
-	232.65	54126.02	0.05	2706.30
-	118.45	14030.40	0.05	701.52
-	170	28900.00	0.05	1445.00
-	132.6	17582.76	0.05	879.14
-	146.65	21506.22	0.05	1075.31
-	101.85	10373.42	0.05	518.67
-	0	0.00	0.05	0.00
-	7.65	58.52	0.05	2.93
-	78.75	6201.56	0.05	310.08
-	157.35	24759.02	0.05	1237.95
-	169.65	28781.12	0.05	1439.06
-	143.15	20491.92	0.05	1024.60
-	120.2	14448.04	0.05	722.40
-	232.05	53847.20	0.05	2692.36

34.20	1169.64	0.05	58.48	-0.09
55.00	3025.00	0.05	151.25	0.23
64.85	4205.52	0.05	210.28	0.10
			778.19	0.94
	Variance=	778.19		
	SD=	27.90%		

210	44100.00	0.05	2205.00
315.85	99761.22	0.05	4988.06
286.25	81939.06	0.05	4096.95
			28397.35
	Variance=	28397.35	
	SD=	168.52%	

CONCLUSION

These ratios also help in industry analysis and in predicting market future, according to the performance of the company. News about the company and the segment in which company/industry is operating are also helpful in predicting company future and there return. Further detailed study of market can be done using these ratios. Relative study can be done to see, in which stock investor must invest, so there is minimum risk in investment in particular stock/segment.

The aforesaid description throws light on the significant ratios namely Risk factor, Intercept, Standard Deviation, Variance, Security Return, P/E ratio, Correlation coefficient and Variation of the five Indian companies – HCL, INFOSYS, TCS, and WIPRO.